## Exploring Trigonometric Ratios for Angles Greater than $90^{\circ}$

## Angles in Standard Position

## standard position

an angle in the Cartesian plane whose vertex lies at the origin and whose initial arm lies on the positive $x$-axis. Angle $\theta$ is measured from the initial arm to the terminal arm.
principal angle ( $\boldsymbol{\theta}$ )
the counter clockwise angle between the initial arm and the terminal arm of an angle in standard position. Its value is between $0^{\circ}$ and $360^{\circ}$.
related acute angle ( $\boldsymbol{\beta}$ )
the acute angle between the terminal arm of an angle in
 standard position and the x-axis when the terminal arm lies in quadrants 2,3 , or 4 . Its value is between $0^{\circ}$ and $90^{\circ}$.

## Investigation

1. Sketch the angles given in the space provided in standard form. Be sure to include the principal angle and the related acute angle for each. Then complete the table that follows.


| Principal <br> Angle <br> $\boldsymbol{\theta}$ | Quadrant <br> $\#$ | Related <br> Acute Angle <br> $\boldsymbol{\beta}$ | $\sin \boldsymbol{\theta}$ | $\boldsymbol{\operatorname { c o s } \theta}$ | $\boldsymbol{\operatorname { t a n } \boldsymbol { \theta }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $45^{\circ}$ | 1 | $45^{\circ}$ | 0.707 | 0.707 | 1 |
| $135^{\circ}$ |  |  |  |  |  |
| $225^{\circ}$ |  |  |  |  |  |
| $315^{\circ}$ |  |  |  |  |  |

2. Sketch the angles given in the space provided in standard form. Be sure to include the principal angle and the related acute angle for each. Then complete the table that follows.


| Principal <br> Angle <br> $\boldsymbol{\theta}$ | Quadrant <br> $\#$ | Related <br> Acute Angle <br> $\boldsymbol{\beta}$ | $\boldsymbol{\operatorname { s i n } \theta}$ | $\cos \theta$ | $\tan \boldsymbol{\theta}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $30^{\circ}$ |  |  |  |  |  |
| $150^{\circ}$ |  |  |  |  |  |
| $210^{\circ}$ |  |  |  |  |  |
| $330^{\circ}$ |  |  |  |  |  |

3. Sketch the angles given in the space provided in standard form. Be sure to include the principal angle and the related acute angle for each. Then complete the table that follows.


| Principal <br> Angle <br> $\boldsymbol{\theta}$ | Quadrant <br> $\#$ | Related <br> Acute Angle <br> $\boldsymbol{\beta}$ | $\sin \theta$ | $\cos \theta$ | $\tan \theta$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $60^{\circ}$ |  |  |  |  |  |
| $120^{\circ}$ |  |  |  |  |  |
| $240^{\circ}$ |  |  |  |  |  |
| $300^{\circ}$ |  |  |  |  |  |

## Investigation Follow-Up

1. Look back at the tables you filled in, and complete the table below by writing the sign (+ or -) on each trigonometric ratio in the given quadrant.

| Trigonometric <br> Ratio | Quadrant |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | I | II | III | IV |  |
| sine |  |  |  |  |  |
| cosine |  |  |  |  |  |
| tangent |  |  |  |  |  |

2. State all the angles between $0^{\circ}$ and $360^{\circ}$ that make each equation true. Verify with your calculator.
a. $\sin 53^{\circ}=\sin$ $\qquad$
b. $\tan 130^{\circ}=-\tan$ $\qquad$
c. $\sin \left(-40^{\circ}\right)=\sin$ $\qquad$ d. $-\cos \left(-113^{\circ}\right)=\cos$ $\qquad$
3. Given some angle $\theta$ where $0 \leq \theta \leq 90$, if $\sin \theta=k$,
a. Determine all angles between 0 and 360 where $\sin \theta=k$.
b. Determine all angles between 0 and 360 where $\sin \theta=-k$.
