

What's Going On?

Checking In

Minds on

Another old friend :)

Action!

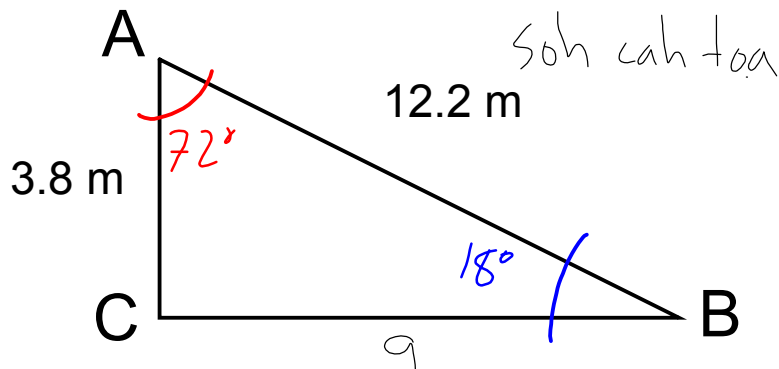
Some new friends!

Consolidation

Using your friends.

Learning Goal - I will know the trig ratios of our special angles and be able to apply operations to them.

Solve the triangle below without using the Pythagorean Theorem.



Angle A

$$\cos A = \frac{3.8}{12.2}$$

$$A = \cos^{-1}\left(\frac{3.8}{12.2}\right)$$

$$A = 72^\circ$$

Angle B

$$\sin B = \frac{3.8}{12.2}$$

$$B = \sin^{-1}\left(\frac{3.8}{12.2}\right)$$

$$B = 18^\circ$$

Now that we have all of the angles, we can solve for the missing side **a** in several ways.

We can use Angle A and tan OR sin

We can use Angle B and tan OR cos

$$\cos 18^\circ = \frac{a}{12.2}$$

$$a = 12.2 \times \cos 18^\circ$$

$$a = 11.6 \text{ m}$$

Minds on

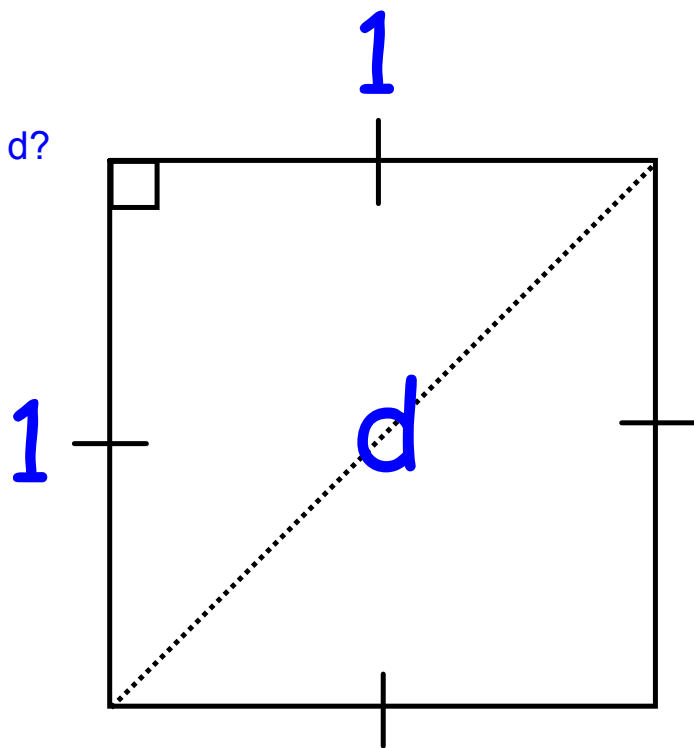
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1. What is the EXACT length of d ?

$$1^2 + 1^2 = d^2$$

$$\sqrt{d^2} = \sqrt{2}$$

$$d = \sqrt{2}$$

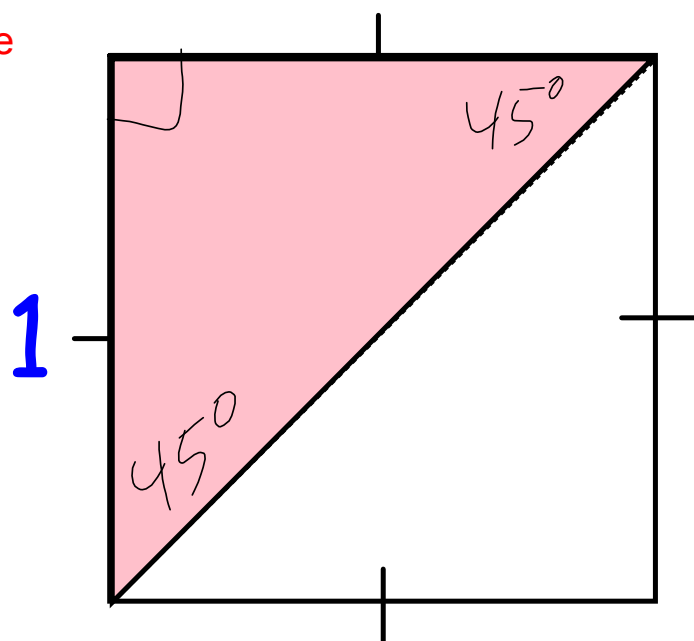


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2 side and

2. What are the measures of the angles in the red triangle?



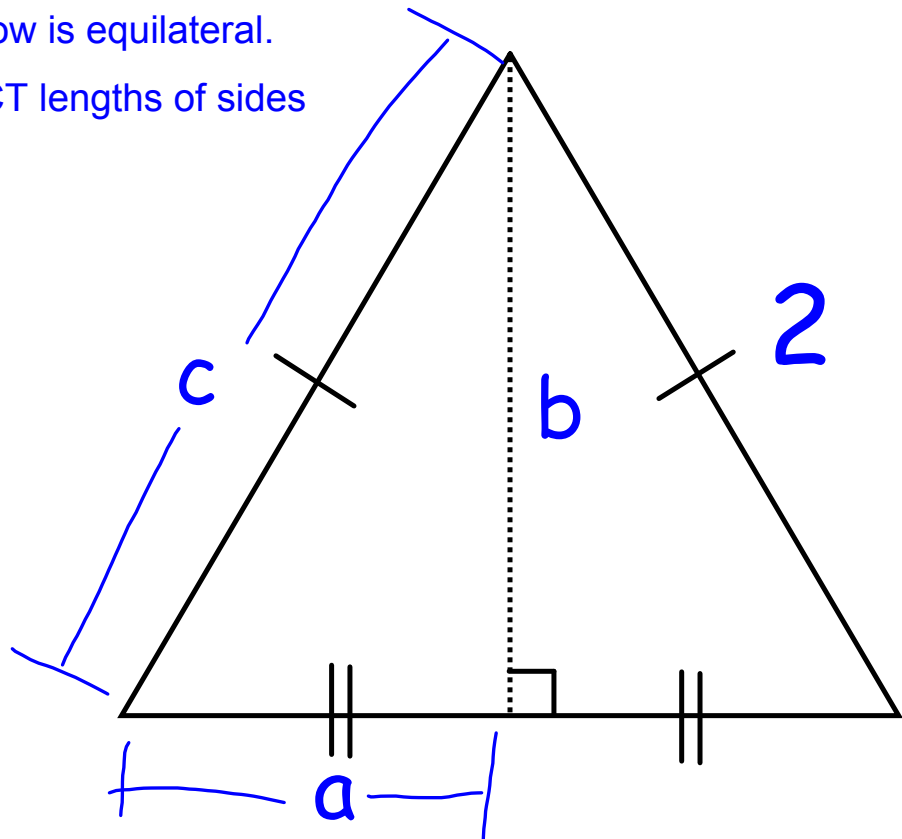
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The large triangle below is equilateral.

1. What are the EXACT lengths of sides a, b and c?

$$\begin{aligned}c &= 2 \\a &= 1 \\a^2 + b^2 &= c^2 \\1^2 + b^2 &= 2^2 \\1 + b^2 &= 4 \\\sqrt{b^2} &= \sqrt{3} \\b &= \sqrt{3}\end{aligned}$$

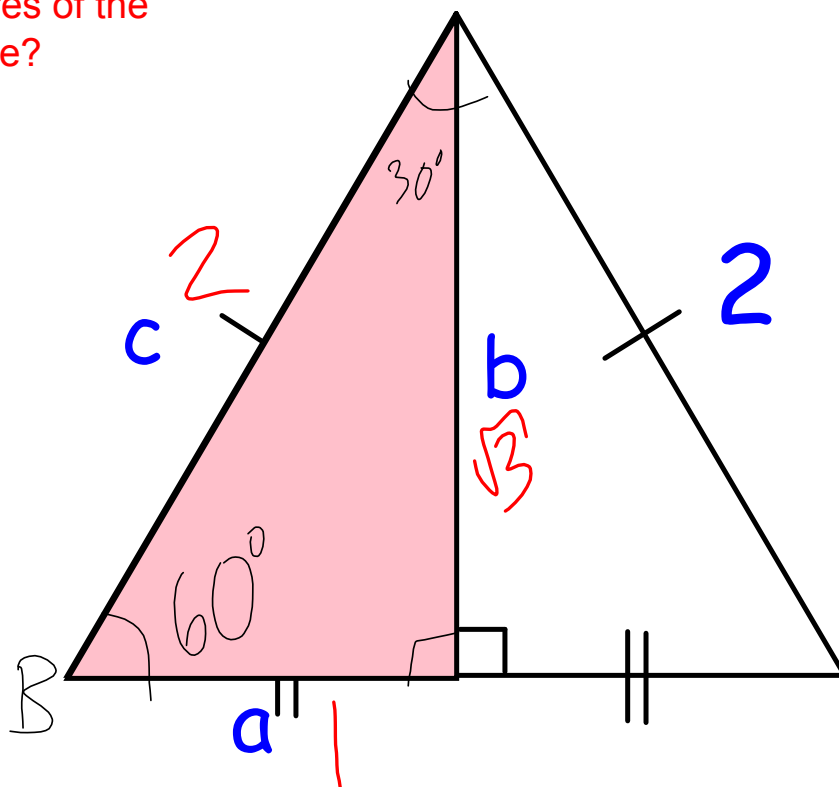


Minds on

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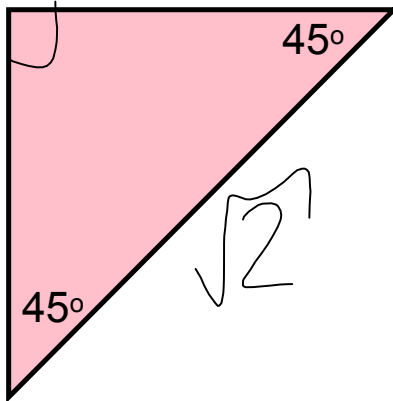
2. What are the measures of the angles in the red triangle?

$$\cos B = \frac{1}{2}$$
$$B = \cos^{-1}\left(\frac{1}{2}\right)$$



Action!

Some New Friends



What are the 6 trigonometric ratios for a 45 degree angle?

Be exact!

$$\sin 45 = \frac{1 \cdot \sqrt{2}}{\sqrt{2} \cdot \sqrt{2}}$$

Rationalize
the denominator

$$= \frac{\sqrt{2}}{2}$$

$$\sin 45 = \frac{\sqrt{2}}{2}$$

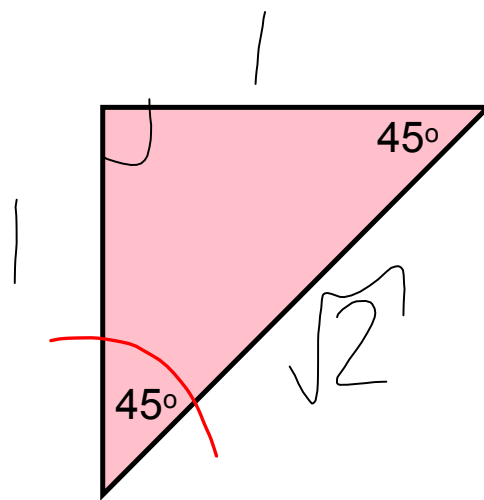
$$\cos 45 =$$

$$\tan 45 =$$

$$\csc 45 =$$

$$\sec 45 =$$

$$\cot 45 =$$



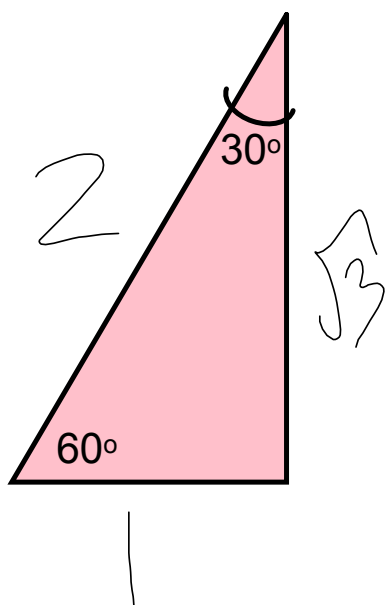
$$\sin 45 = \frac{\sqrt{2}}{2} \quad \cos 45 = \frac{\sqrt{2}}{2}$$

$$\tan 45 = 1 \quad \csc 45 = \sqrt{2}$$

$$\sec 45 = \sqrt{2} \quad \cot 45 = 1$$

Action!

Some New Friends



What are the 6 trigonometric ratios for a 30 degree and a 60 degree angle?

Be exact!

*No radicals allowed in the denominator!

$$\sin 30 =$$

$$\cos 30 =$$

$$\tan 30 =$$

$$\csc 30 =$$

$$\sec 30 =$$

$$\cot 30 =$$

$$\sin 60 =$$

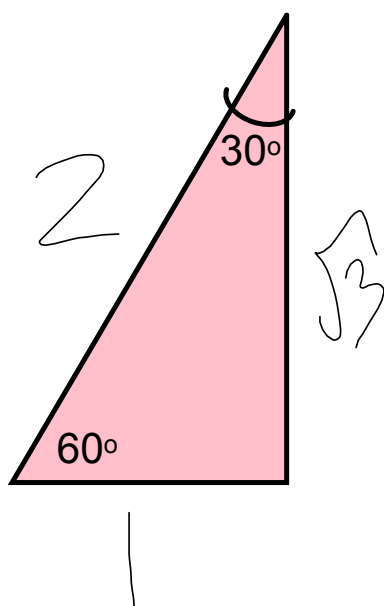
$$\cos 60 =$$

$$\tan 60 =$$

$$\csc 60 =$$

$$\sec 60 =$$

$$\cot 60 =$$



$$\sin 30 = \frac{1}{2}$$

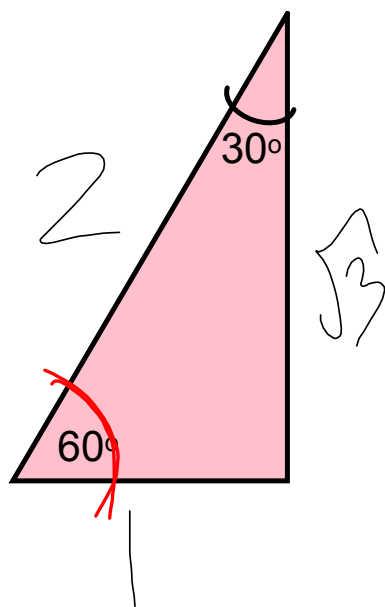
$$\cos 30 = \frac{\sqrt{3}}{2}$$

$$\tan 30 = \frac{\sqrt{3}}{3}$$

$$\csc 30 = 2$$

$$\sec 30 = \frac{2\sqrt{3}}{3}$$

$$\cot 30 = \sqrt{3}$$



$$\frac{2}{\sqrt{3}} \quad \frac{\sqrt{3}}{\sqrt{3}} \quad \frac{2\sqrt{3}}{3}$$

$$\sin 60 = \frac{\sqrt{3}}{2}$$

$$\csc 60 = \frac{2\sqrt{3}}{3}$$

$$\cos 60 = \frac{1}{2}$$

$$\sec 60 = 2$$

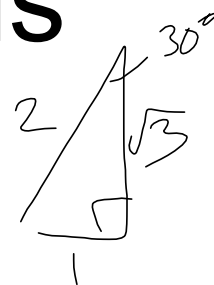
$$\tan 60 = \sqrt{3}$$

$$\cot 60 = \frac{\sqrt{3}}{3}$$

Consolidation

Using your friends

Determine the exact value of:



$$(\sin 45^\circ)(\cos 45^\circ) + (\sin 30^\circ)(\sin 60^\circ)$$

$$= \left(\frac{\sqrt{2}}{2} \right) \left(\frac{\sqrt{2}}{2} \right) + \left(\frac{1}{2} \right) \left(\frac{\sqrt{3}}{2} \right)$$

$$= \frac{2}{4} + \frac{\sqrt{3}}{4}$$

$$= \frac{2 + \sqrt{3}}{4}$$

