First, it's handy to know what each of our parent functions looks like in this form:

Quadratic: 
$$f(x) = x^2$$
 Square Root:  $f(x) = \sqrt{x}$  
$$g(x) = a[k(x-d)]^2 + c \qquad g(x) = a\sqrt{k(x-d)} + c$$
 Reciprocal:  $f(x) = \frac{1}{x}$  Absolute Value:  $f(x) = |x|$  
$$g(x) = a\left(\frac{1}{k(x-d)}\right) + c \qquad g(x) = a|k(x-d)| + c$$

We also need to understand what each of our *parameters* (*a*, *k*, *d* and *c*) do.

You should already have a pretty good grasp on a, d and c from Grade 10. Although d and c were represented by different letters, the roles that they play have not changed! And if you understand what a does, figuring out b should be no problem at all!

| The effects of the parameters <b>a</b> , <b>k</b> , <b>d</b> and <b>c</b>         |  |
|---|--|
| a: reflection in the x-axis - when a is negative                                  | <b>k</b> : reflection in the y-axis* - when k is negative  |
| vertical stretch or compression - stretch when  a  > 1 - compression when  a  < 1 | horizontal stretch or compression - compression when  k  > 1 - stretch when  k  < 1  |
| C: vertical translation - up when c is positive - down when c is negative         | *If already symmetrical about y-axis, reflection does nothing!  d: horizontal translation  - to the right when d is positive  - to the left when d is negative |

As you likely already understand, if we have several parameters applied to our function at once it <u>may</u> experience changes in shape, orientation and location!

## Applying Transformations to a Graph (see Example 1 on Page 61-63)

The order that you apply transformations to a parent function is important.

## Always apply **a** and **k** before **c** and **d**!

From a table of values or a graph (it will be helpful to create a table of values)

- 1. Apply any horizontal stretches or compressions.
  - Divide the x-coordinates of your original points by the value of k
- 2. Apply any vertical stretches or compressions.
  - Multiply the y-coordinates of your "new" points by the value of a
- 3. Apply any reflections in the x-axis or y-axis
  - Flip graph over the y-axis if k is negative. (change the sign on your "new" x-coordinates)
  - Flip graph over the x-axis if **a** is negative. (change the sign on your "new" y-coordinates)
- 4. Apply any horizontal shifts.
  - Shift the graph to the <u>right</u> if **d** is <u>positive</u> or to the <u>left</u> if **d** is <u>negative</u>.
    - Add d to each x-coordinate if d is positive
    - o Subtract **d** from each x-coordinate if **d** is negative
- 5. Apply any vertical shifts.
  - Shift the graph up if **c** is positive or down if **c** is negative.
    - o Add **c** to each y-coordinate if **c** is positive
    - Subtract c from each y-coordinate if c is negative

## Applying Transformations to an Equation (see Example 2 on Page 64-65)

The key to this is simply identifying the value of each parameter.

## If you are told to apply:

- A <u>horizontal stretch</u> by a factor of 3;  $k = \frac{1}{3}$ .

- A <u>horizontal compression</u> by a factor of  $\frac{1}{3}$ ; k = 3.

This is why we **divide** our x-coordinates by the value of k!

- A <u>vertical stretch</u> by a factor of 5;  $\alpha = 5$ .
- A <u>vertical compression</u> by a factor of  $\frac{1}{5}$ ;  $\boldsymbol{a} = \frac{1}{5}$ .
- A <u>reflection in the y-axis</u>; **k** is negative.
- A <u>reflection in the x-axis</u>; a is negative.
- A translation 2 units up and 3 units left; c = 2 and d = -3.
- A translation 1 unit down and 4 units right; c = -1 and d = 4