First, it's handy to know what each of our parent functions looks like in this form:

$$
\begin{array}{c|c}
\text { Quadratic: } f(x)=x^{2} & \text { Square Root: } f(x)=\sqrt{x} \\
\boldsymbol{g}(\boldsymbol{x})=\boldsymbol{a}[\boldsymbol{k}(\boldsymbol{x}-\boldsymbol{d})]^{2}+\boldsymbol{c} & \boldsymbol{g}(\boldsymbol{x})=\boldsymbol{a} \sqrt{\boldsymbol{k}(\boldsymbol{x}-\boldsymbol{d})}+\boldsymbol{c} \\
\text { Reciprocal: } f(x)=\frac{1}{x} & \text { Absolute Value: } f(x)=|x| \\
\boldsymbol{g}(\boldsymbol{x})=\boldsymbol{a}\left(\frac{1}{\boldsymbol{k}(\boldsymbol{x}-\boldsymbol{d})}\right)+\boldsymbol{c} & \boldsymbol{g}(\boldsymbol{x})=\boldsymbol{a}|\boldsymbol{k}(\boldsymbol{x}-\boldsymbol{d})|+\boldsymbol{c}
\end{array}
$$

We also need to understand what each of our parameters ( $\boldsymbol{a}, \boldsymbol{k}, \boldsymbol{d}$ and $\boldsymbol{c}$ ) do.
You should already have a pretty good grasp on $\boldsymbol{a}, \boldsymbol{d}$ and $\boldsymbol{c}$ from Grade 10. Although $\boldsymbol{d}$ and $\boldsymbol{c}$ were represented by different letters, the roles that they play have not changed!
And if you understand what $\boldsymbol{a}$ does, figuring out $\boldsymbol{k}$ should be no problem at all!

| The effects of the parameters $\boldsymbol{a}, \boldsymbol{k}, \boldsymbol{d}$ and $\boldsymbol{c}$ |  |
| :---: | :---: |
| a: reflection in the $x$-axis <br> - when a is negative <br> vertical stretch or compression <br> - stretch when $\|a\|>1$ <br> - compression when $\|a\|<1$ | $\mathbf{k}$ : reflection in the $y$-axis* <br> - when $k$ is negative <br> horizontal stretch or compression <br> - compression when $\|\mathrm{k}\|>1$ <br> - stretch when $\|\mathrm{k}\|<1$ <br> *If already symmetrical about $y$-axis, reflection does nothing! |
| C: vertical translation <br> - up when c is positive <br> - down when c is negative | d: horizontal translation <br> - to the right when $d$ is positive <br> - to the left when $d$ is negative |

As you likely already understand, if we have several parameters applied to our function at once it may experience changes in shape, orientation and location!

## Applying Transformations to a Graph (see Example 1 on Page 61-63)

The order that you apply transformations to a parent function is important.
Always apply $\boldsymbol{a}$ and $\boldsymbol{k}$ before $\boldsymbol{c}$ and $\boldsymbol{d}$ !
From a table of values or a graph (it will be helpful to create a table of values)

1. Apply any horizontal stretches or compressions.

- Divide the x-coordinates of your original points by the value of $\boldsymbol{k}$

2. Apply any vertical stretches or compressions.

- Multiply the y-coordinates of your "new" points by the value of $\boldsymbol{a}$

3. Apply any reflections in the $\mathbf{x}$-axis or $\mathbf{y}$-axis

- Flip graph over the $\boldsymbol{y}$-axis if $\boldsymbol{k}$ is negative. (change the sign on your "new" $x$-coordinates)
- Flip graph over the x-axis if $\boldsymbol{a}$ is negative. (change the sign on your "new" $y$-coordinates)

4. Apply any horizontal shifts.

- Shift the graph to the right if $\boldsymbol{d}$ is positive or to the left if $\boldsymbol{d}$ is negative.
- Add $\boldsymbol{d}$ to each $x$-coordinate if $\boldsymbol{d}$ is positive
- Subtract $\boldsymbol{d}$ from each $x$-coordinate if $\boldsymbol{d}$ is negative

5. Apply any vertical shifts.

- Shift the graph up if $\boldsymbol{c}$ is positive or down if $\boldsymbol{c}$ is negative.
- Add $\boldsymbol{c}$ to each $y$-coordinate if $\boldsymbol{c}$ is positive
- Subtract $\boldsymbol{c}$ from each y -coordinate if $\boldsymbol{c}$ is negative


## Applying Transformations to an Equation (see Example 2 on Page 64-65)

The key to this is simply identifying the value of each parameter.
If you are told to apply:

- A horizontal stretch by a factor of $3 ; \boldsymbol{k}=\frac{1}{3}$.

- A horizontal compression by a factor of $\frac{1}{3} ; \boldsymbol{k}=3$.

This is why we divide our x-coordinates by the value of $\boldsymbol{k}$ !

- A vertical stretch by a factor of $5 ; \boldsymbol{a}=5$.
- A vertical compression by a factor of $\frac{1}{5}$; $\boldsymbol{a}=\frac{1}{5}$.
- A reflection in the $y$-axis; $\boldsymbol{k}$ is negative.
- A reflection in the x-axis; $\boldsymbol{a}$ is negative.
- A translation 2 units up and 3 units left; $\boldsymbol{c}=2$ and $\boldsymbol{d}=-3$.
- A translation 1 unit down and 4 units right; $\boldsymbol{c}=-1$ and $\boldsymbol{d}=4$

